

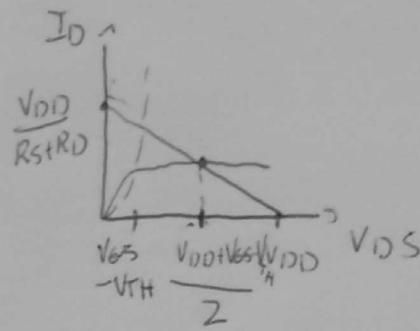
$$A_v = 5$$

$$\mu_n C_{ox} = 100 \mu A/V$$

$$V_{TH} = 0,5V$$

$$\frac{W}{L} = 244$$

$$Z_{in} = 45,5 \Omega$$



$$1,8 + R_D I_D + R_S I_D + V_{DS} = 0 \Rightarrow V_{DS} = \underset{V_{DD}}{1,8} - I_D \cdot (R_D + R_S) \quad (1)$$

$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2 \quad (2)$$

$$V_{DS} = \frac{V_{DD} + V_{GS} - V_{TH}}{2} \quad (3)$$

$$\begin{cases} A_v = g_m R_D \rightarrow \text{Verp qmos sinais} \\ g_m = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH}) \end{cases} \Rightarrow R_D = \frac{A_v}{\mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})} \quad (4)$$

$$Z_{in} = R_S \parallel \frac{1}{g_m} \approx \text{Verp qmos sinais} = \frac{1}{\frac{1}{R_S} + g_m} = \frac{R_S}{R_S + \frac{1}{g_m}} \quad \text{with } \frac{1}{g_m} = r_m$$

$$\Rightarrow Z_{in} R_S + Z_{in} r_m = R_S r_m \Rightarrow R_S (r_m - Z_{in}) = Z_{in} r_m$$

$$R_S = \frac{Z_{in} r_m}{r_m - Z_{in}} = \frac{Z_{in}}{\frac{1}{g_m} - Z_{in}} = \frac{Z_{in}}{\frac{1 - g_m Z_{in}}{g_m}}$$

$$R_S = \frac{Z_{in}}{1 - g_m Z_{in}} \quad (5)$$

$$g_m = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH}) \quad (6)$$

$$(6) \rightarrow (5)$$

$$R_S = \frac{Z_{in}}{1 - Z_{in} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})} \quad (7)$$

$$(1) = (3)$$

$$V_{DD} - I_D (R_D + R_S) = \frac{V_{DD} + V_{GS} - V_{TH}}{2} \Rightarrow 2V_{DD} - 2I_D (R_D + R_S) = V_{DD} + V_{GS} - V_{TH}$$

$$\rightarrow V_{DD} - V_{GS} + V_{TH} - 2I_D (R_D + R_S) = 0 \quad (8)$$

$$(2), (4) \text{ e } (7) \rightarrow (8)$$

$$V_{DD} - V_{GS} + V_{TH} - 2 \cdot \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2 \left[\frac{A_v}{\mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})} + \frac{Z_{in}}{1 - Z_{in} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})} \right] = 0$$

$$V_{DD} - V_{GS} + V_{TH} - (V_{GS} - V_{TH}) \cdot \frac{A_v}{\mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})} - \frac{Z_{in} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2}{1 - Z_{in} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})} = 0$$

\downarrow 1,8 \downarrow 0,5 \downarrow X \downarrow 5 \downarrow 45,5 \cdot 10^3 \frac{1}{L}

$$V_{DD} - (V_{GS} - V_{TH})(A_{\sigma} + 1) - \frac{z_{in} \cdot K (V_{GS} - V_{TH})^2}{1 - z_{in} K (V_{GS} - V_{TH})} = 0$$

\downarrow $\frac{\mu_n \epsilon_{ox} W}{L}$ \downarrow X

$$V_{DD} - (V_{GS} - V_{TH})(A_{\sigma} + 1)X - \frac{z_{in} K X^2}{1 - z_{in} K X} = 0$$

$$\frac{V_{DD} \cdot (1 - z_{in} K X) - (A_{\sigma} + 1) X (1 - z_{in} K X) - z_{in} K X^2}{1 - z_{in} K X} = 0$$

$$V_{DD} - (V_{DD} z_{in} K X) - (A_{\sigma} + 1) X + (A_{\sigma} + 1) z_{in} K X^2 - z_{in} K X^2 = 0$$

$$z_{in} K (A_{\sigma} + 1) X^2 - (V_{DD} z_{in} K + A_{\sigma} + 1) X + V_{DD} = 0$$

\downarrow 45,5 \downarrow 0,0244 \downarrow 5 \downarrow 1,8 \downarrow 45,5 \downarrow 5 \downarrow 1,8

$$5,5510 X^2 - 7,9984 X + 1,8 = 0$$

$$X = \begin{cases} 1,1618 V \\ 0,2791 V \end{cases} \quad \begin{matrix} V_{GS} = X + V_{TH} \\ \Rightarrow \\ V_{GS} = \begin{cases} 1,6618 V \\ 0,7791 V \end{cases} \end{matrix}$$

$$\textcircled{2} \Rightarrow \begin{cases} 16,4666 \text{ mA} \\ 0,9504 \text{ mA} \end{cases} \} I_D$$

$$\textcircled{6} \Rightarrow \begin{cases} 28,3473 \text{ mS} \\ 6,8104 \text{ mS} \end{cases} \} g_m$$

$$\textcircled{4} \Rightarrow R_D \begin{cases} 176,3838 \Omega \\ 734,1763 \Omega \end{cases}$$

$$\textcircled{5} \Rightarrow R_S \begin{cases} -157,0043 \Omega = \tilde{M}OK \\ 65,9297 \Omega \end{cases}$$

$$\bullet V_G S = V_G - V_S \Rightarrow 0,7791 = V_G - \underset{63,92}{R_S} \cdot \underset{0,4504 \text{mA}}{I_D}$$

$$\Rightarrow \boxed{V_G = 0,8418 \text{V}}$$

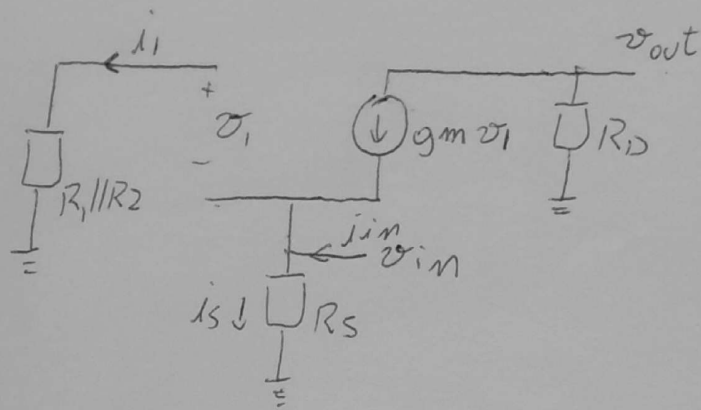
$$\bullet V_G = \frac{R_2}{R_1 + R_2} \cdot V_{DD} \Rightarrow 0,8418 = \frac{R_2}{R_1 + R_2} \cdot 1,8$$

$$\Rightarrow 0,3418(R_1 + R_2) = R_2 \cdot 1,8$$

$$\Rightarrow R_1 = 1,383 \cdot R_2$$

$$\bullet \text{ Fazendo } \boxed{R_2 = 10 \text{k}\Omega} \Rightarrow \boxed{R_1 = 11,383 \text{k}\Omega}$$

• Modelo de pequenos sinais



• $v_{out} = -g_{m1} v_1 R_D$

$\Rightarrow A_v = +g_{m1} R_D$

• $v_{in} = -v_1$, pois $i_1 = \phi$

• $i_s = i_{in} + g_{m1} v_1 \Rightarrow \frac{v_{in}}{R_S} = i_{in} + g_{m1} v_1 \Rightarrow i_{in} = -v_1 \cdot \left(\frac{1}{R_S} + g_{m1} \right)$

$Z_{in} = \left(\frac{1}{R_S} + g_{m1} \right)^{-1} = R_S // \frac{1}{g_{m1}}$

• $Z_{out} \Rightarrow v_{in} = \phi \Rightarrow V_1 = \phi \Rightarrow R_{out} = R_D$