

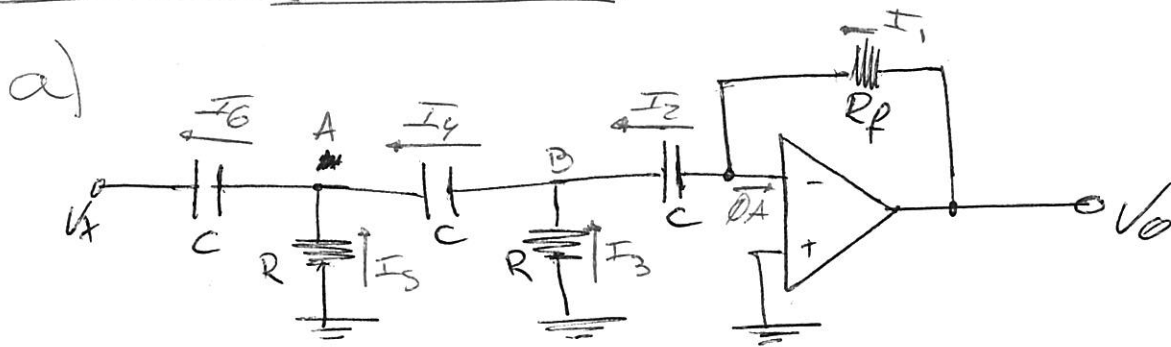
13.4 SEDRA (5º ed)

$$a) \frac{R_F}{R_A} = 2 \Rightarrow \frac{10 + X}{50 - X} = 2 \Rightarrow X = 30$$

Portanto R_A deve ser $(50 - 30)k\Omega = 20k\Omega$, logo o potenciômetro deve ser posicionado em $20k\Omega$ PARA O TERRA.

$$b) f = \frac{1}{2\pi RC} = \frac{1}{2\pi \cdot 10 \cdot 10^3 \cdot 16 \cdot 10^{-9}} \Rightarrow \boxed{f = 1 \text{ kHz}}$$

13.5 e 6 SEDRA (5º ed)



$$I_1 = \frac{V_o}{R_f}$$

$$V_B = 0 - \frac{I_2}{sC} = -\frac{I_1}{sC} \quad (I_2 = I_1) = -\frac{1}{sC} \left(\frac{V_o}{R_f} \right) = -\frac{V_o}{sCR_f}$$

$$\bullet I_3 = 0 - \frac{V_B}{R} = \frac{V_o}{sCR_f}$$

$$\bullet V_A = V_B - \frac{I_4}{sC} = -\frac{V_o}{sCR_f} - \frac{1}{sC} (I_3 + I_2) = -\frac{V_o}{sCR_f} - \frac{1}{sC} \left(\frac{V_o}{sCR_f R} + \frac{V_o}{R_f} \right)$$

$$\bullet I_S = \frac{0 - V_A}{R} = \frac{V_o}{sCR_f R} + \frac{1}{sCR} \left(\frac{V_o}{sCR_f R} + \frac{V_o}{R_f} \right)$$

$$\bullet I = I_G = I_5 + I_4 = I_5 + I_3 + I_2 = I_5 + I_3 + I_1$$

• Substituindo, temos:

$$I = \frac{V_0}{sCRpR} \left(2 + \frac{1}{sCR} \right) + \frac{V_0}{R_f} \left(1 + \frac{1}{sCR} \right)$$

$$\bullet V_x = V_{OA} - \frac{I_G}{sC} = V_{OA} - \frac{I}{sC}$$

• Substituindo V_A e I , temos:

$$V_x = -\frac{V_0}{sCR_f} \left[3 + \frac{4}{sCR} + \frac{1}{s^2C^2R^2} \right] = \boxed{-\frac{V_0}{j\omega CR_f} \left[3 + \frac{4}{j\omega CR} - \frac{1}{\omega^2 C^2 R^2} \right]}$$

$$b.) A\beta = \frac{V_0}{V_x} = \frac{-j\omega CR_f}{\left[3 + \frac{4}{j\omega CR} - \frac{1}{\omega^2 C^2 R^2} \right]} = \frac{\omega^2 C^2 R \cdot R_f}{4 + j \left(3\omega CR - \frac{1}{\omega CR} \right)}$$

Condições para oscilação:

$$|A\beta| = 1, \angle A\beta = 0^\circ \text{ ou } 360^\circ$$

$$\bullet \angle A\beta = 0^\circ \Rightarrow \angle \frac{\omega^2 C^2 R \cdot R_f}{4 + j \left(3\omega CR - \frac{1}{\omega CR} \right)} = 0^\circ \Rightarrow 0^\circ - \tan^{-1} \left(\frac{3\omega CR - \frac{1}{\omega CR}}{4} \right) = 0^\circ$$

$$\Rightarrow 3\omega CR - \frac{1}{\omega CR} = 0 \Rightarrow \omega_0 = \frac{1}{CR\sqrt{3}} = \frac{1}{16 \cdot 10^{-9} \cdot 10 \cdot 10^3 \sqrt{3}}$$

$$\Rightarrow \boxed{\omega_0 = 574,3 \text{ Hz}}$$

$$c) |A| \geq 1 \rightarrow \left| \frac{\omega_0^2 \cdot C^2 \cdot R \cdot R_f}{4 + j \left(3\omega_0 C R - \frac{1}{\omega_0 C R} \right)} \right| \geq 1$$

Substituindo ω_0 , temos:

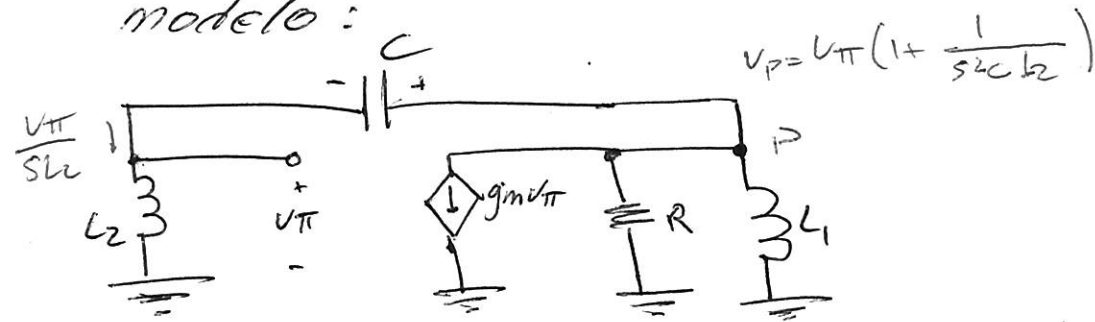
$$\left| \frac{\left(\frac{1}{C R \sqrt{3}} \right)^2 \cdot C^2 \cdot R \cdot R_f}{4 + j \left(3 \frac{1}{C R \sqrt{3}} C R - \frac{1}{\left(\frac{1}{C R \sqrt{3}} \right) C R} \right)} \right| \geq 1 \Rightarrow \frac{1}{3} \left(\frac{R_f}{R} \right) \geq 4$$

$$\Rightarrow R_f \geq 12R \Rightarrow R_f = 12R \Rightarrow R_f = 12 \cdot 10 \cdot 10^3 \Rightarrow \boxed{R_f = 120 \text{ k}\Omega}$$

Portanto, o ponto mínimo é com o potenciômetro em 20 k Ω

13.8 SEDRA 5ª ed

modelo:



$$V_p = V_{\pi} + V_C = V_{\pi} + \frac{1}{sC} \cdot \frac{V_{\pi}}{sL_2} = V_{\pi} \left(1 + \frac{1}{s^2 C L_2} \right)$$

Corrente no P:

$$\frac{V_{\pi}}{sL_2} + g_m V_{\pi} + \left(\frac{1}{sL_1} + \frac{1}{R} \right) V_p = 0$$

• Como $V_{\pi} \neq 0$, divide por V_{π} :

$$\frac{1}{sL_2} + g_m + \left(\frac{1}{sL_1} + \frac{1}{R} \right) \left(1 + \frac{1}{s^2 C L_2} \right) = 0$$

• Substituindo $s = j\omega$, temos:

$$\left(g_m + \frac{1}{R} - \frac{1}{\omega^2 R C L_2} \right) + j \left(\frac{1}{\omega C L_1 L_2} - \frac{1}{\omega L_1} - \frac{1}{\omega L_2} \right) = 0$$

• Para oscilação iniciar tanto a parte real como imaginária deve ser zero:

→ fazendo a parte imaginária igual a zero, temos:

$$\omega_0 = \sqrt{\frac{1}{(L_1 + L_2)C}}$$

• Para oscilar, impomos $|A\beta| \geq 1$:

→ Substituindo ω_0 ~~no~~ ~~para~~, temos:

$$\left| \left(g_m + \frac{1}{R} - \frac{1}{\omega_0^2 R C L_2} \right) + j \left(\frac{1}{\omega_0 C L_2} - \frac{1}{\omega_{L1}} - \frac{1}{\omega_{L2}} \right) \right| \geq 1$$

$$g_m + \frac{1}{R} - \frac{C(L_1 + L_2)}{R C L_2} \geq 1$$

$$\therefore \boxed{g_m R \geq \frac{L_1}{L_2}}$$

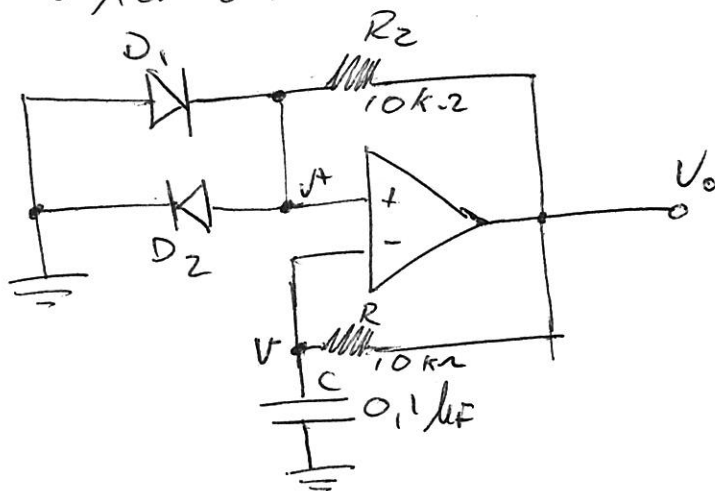
13.16 (SEBRA Soed)

- $T = 2RC \ln \left(\frac{1+\beta}{1-\beta} \right) \rightarrow T = 2 \cdot 1 \cdot 10^6 \cdot 0,1 \cdot 10^{-6} \ln \left(\frac{1+0,09}{1-0,09} \right) = 3,6 \text{ms}$
- $\beta = \frac{R_1}{R_1+R_2} = \frac{100 \text{k}\Omega}{100 \text{k}\Omega + 1 \text{M}\Omega} = 0,09$

$$f = \frac{1}{T} = \frac{1}{3,6 \text{ms}} \Rightarrow \boxed{f = 274 \text{Hz}}$$

13.17 (SEBRA Soed)

• Circuito modificado:



- $V^+ = \beta V^- = V_D \Rightarrow \beta = \frac{V_D}{V^-} = \frac{V_D}{12}$

- $T = 2RC \ln \left(\frac{1+\beta}{1-\beta} \right) = 2 \cdot 10 \cdot 10^3 \cdot 0,1 \cdot 10^{-6} \ln \left(\frac{1 + \frac{V_D}{12}}{1 - \frac{V_D}{12}} \right)$

$$T = 0,002 \ln \left(\frac{12 + V_D}{12 - V_D} \right)$$

- $f = \frac{1}{T} = \frac{1}{0,002 \ln \left(\frac{12 + V_D}{12 - V_D} \right)}$

$$\Rightarrow \boxed{f = \frac{500}{\ln \left(\frac{12 + V_D}{12 - V_D} \right)}}$$

- Considerando que a 25°C , $V_D = 0,7\text{V}$ e que V_D cai 2mV a cada 1°C que aumenta:

→ PARA 0°C :

$$V_D = 0,7 + -2 \cdot 10^{-3} \cdot (0 - 25) = 0,75\text{V}$$

$$f = \frac{500}{\ln\left(\frac{12+0,75}{12-0,75}\right)} \Rightarrow \boxed{f(0^{\circ}\text{C}) = 3995\text{Hz}}$$

→ PARA 25°C :

$$V_D = 0,7 + -2 \cdot 10^{-3} \cdot (25 - 25) = 0,7\text{V}$$

$$f = \frac{500}{\ln\left(\frac{12+0,7}{12-0,7}\right)} \Rightarrow \boxed{f(25^{\circ}\text{C}) = 4281\text{Hz}}$$

→ PARA 50°C

$$V_D = 0,7 + -2\text{mV} \cdot (50 - 25) = 0,65\text{V}$$

$$f = \frac{500}{\ln\left(\frac{12+0,65}{12-0,65}\right)} \Rightarrow \boxed{f(50^{\circ}\text{C}) = 4611\text{Hz}}$$

→ PARA 100°C

$$V_D = 0,7 + -2\text{mV} \cdot (100 - 25) = 0,55\text{V}$$

$$f = \frac{500}{\ln\left(\frac{12+0,55}{12-0,55}\right)} \Rightarrow \boxed{f(100^{\circ}\text{C}) = 5451\text{Hz}}$$

13.18 (SEDRA 5ª ed)

$$\bullet T = \frac{1}{f} = \frac{1}{1 \cdot 10^3} = 1 \text{ ms}$$

$$\bullet T = T_1 + T_2 = RC \left(\frac{V_{TH} - V_{TL}}{L_+} \right) + RC \left(\frac{V_{TH} - V_{TL}}{-L_-} \right)$$

$$L_+ = -L_- : T = 2RC \left(\frac{V_{TH} - V_{TL}}{L_+} \right)$$

- Sendo $V_{PP} = 10V$, $V_{TH} = +5V$ e $V_{TL} = -5V$, temos:
substituindo em T :

$$1 \cdot 10^{-3} = 2(0,01 \cdot 10^{-6})R \left(\frac{5 + (-5)}{10} \right) \Rightarrow \boxed{R = 50k\Omega}$$

$$\bullet V_{TH} = -L_- \left(\frac{R_1}{R_2} \right) \Rightarrow 5 = 10 \cdot \left(\frac{10 \cdot 10^3}{R_2} \right) \Rightarrow \boxed{R_2 = 20k\Omega}$$